

Name \_\_\_\_\_

---

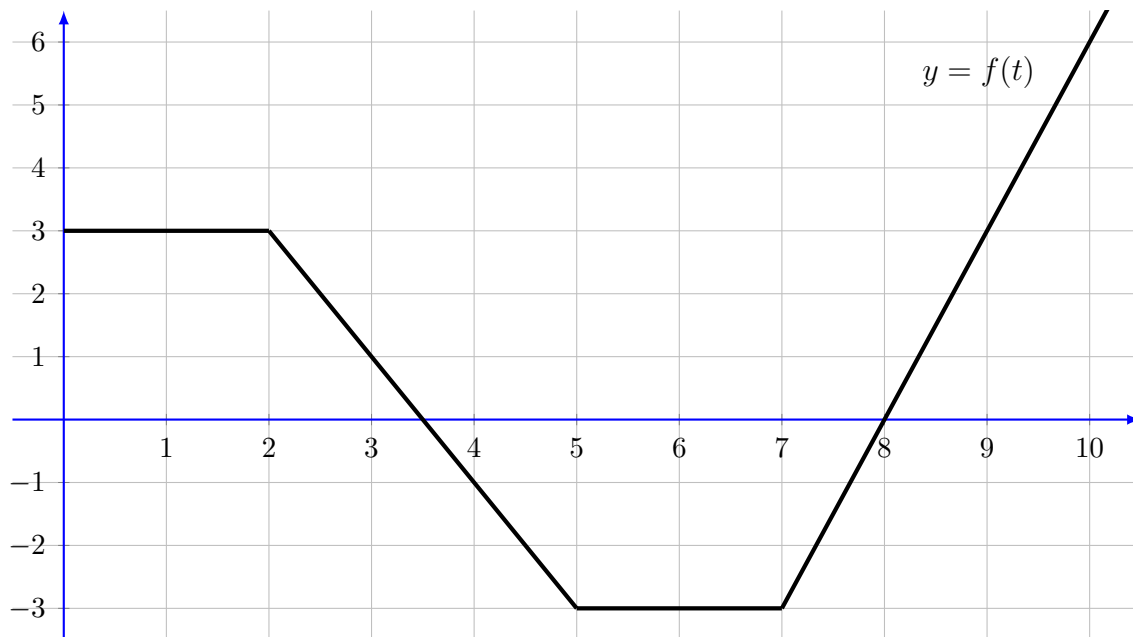
1	
2	
3	
4	
5	
6	

7	
8	
9	
10	
11	
12	
13	
14	
15	
16	

**Part I: Use the picture**

The graph of a function  $f$  is sketched below. Define an “Area function”  $A$  by

$$A(x) = \int_2^x f(t) dt$$



Use the picture and the definition of  $A$  to answer these questions:

1. What is  $A(0)$ ?
2. What is  $A(2)$ ?
3. What is  $A(4)$ ?
4. Where is  $A$  increasing?
5. Where is the minimum of  $A$ ?
6. Where is  $A$  concave up?

**Part II: Matching**

Match the expression on the left with the appropriate choice on the right. Put the letter of the choice on the answer sheet.

$$7. \int_0^8 |2x - 6| dx \qquad (a) 34$$

$$8. \int_0^2 2x^2 - 3 dx \qquad (b) -\frac{2}{3}$$

$$9. \int_0^1 x + \sqrt{1 - x^2} dx \qquad (c) \frac{\pi + 2}{4}$$

$$10. \int_0^{\frac{\sqrt{\pi}}{2}} 2x \sin(x^2) dx \qquad (d) 1 - \frac{1}{\sqrt{2}}$$

$$11. \lim_{n \rightarrow \infty} \sum_{i=1}^n \left(\frac{i}{n}\right)^2 \left(\frac{1}{n}\right) \qquad (e) \frac{1}{3}$$

**Part III: True or False**

12. The function  $g$  defined by  $g(x) = \int_0^x \sin(t^2) dt$  has an absolute maximum at  $x = \sqrt{2\pi}$ .

13.  $\frac{d}{dx} \left( \int_1^3 \sin(t^2) dt \right) = 0$ .

14. If  $f'$  is continuous, then  $\int_1^3 f'(v) dv = f(3) - f(1)$ .

15. If  $f$  and  $g$  are integrable on the interval  $[a, b]$  then

$$\int_a^b f(x)g(x) dx = \left( \int_a^b f(x) dx \right) \left( \int_a^b g(x) dx \right).$$

16. If  $f$  and  $g$  are integrable on the interval  $[a, b]$  then

$$\int_a^b [5f(x) + g(x)] dx = 5 \int_a^b f(x) dx + \int_a^b g(x) dx.$$