## MATH 634, Spring 2014 HOMEWORK 15 due 5:00PM on Monday, May 5.

 $15 \mathbf{D}^*.$  Work to understand the following definitions.

- It is not required to turn in written descriptions.
  - MIN CUT (aka minimum *st*-cut)
  - flow companion graph
  - flow augmenting path
- **15GS.** Run the Gale-Shapley algorithm twice on the following sets of preferences, once with the people proposing, and once with the pets proposing. Discuss how your results are related to the theorems on optimality and pessimality.

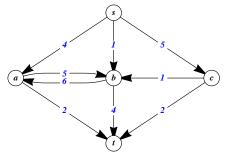
## Pets' Preferences Art Bettie Casper Delphi Ernie 1st Choice F F G Η G 2nd Choice G Η Ι Η F Ι F 3rd Choice Ι J Ι 4th Choice J G Η Ι G 5th Choice Η J J F J

## People's Preferences

	Fei	Georg	Helen	Ivan	Jin
1st Choice	С	Ε	А	Ε	В
2nd Choice		В	D	$\mathbf{C}$	D
3rd Choice	Ε	С	В	А	А
4th Choice	А	А	Ε	В	С
5th Choice	D	D	С	D	Ε

- **15ST.** (a) List all *st*-cuts in the network pictured below (there are eight). Find the capacity of each *st*-cut and determine the min cut from this information.
  - (b) Find a maximum flow for the network (and verify that it is a max flow). Then verify that the max flow / min cut theorem holds.

[Important: Do NOT use the Ford-Fulkerson algorithm in this problem.]



**15FF.** Use the Ford-Fulkerson algorithm to find the max flow and min cut on the attached network. You must prove that your flow is a max flow and your *st*-cut is a min cut.

