

Evaluation of Mathematical Models

In what ways can a model be “good”? A model can be...

▶ **Accurate**

- ▶ Is the output of the model very near to correct?

▶ **Descriptively Realistic**

- ▶ Is the model based on assumptions which are correct?

▶ **Precise**

- ▶ Are the predictors of the model definite numbers?

▶ **Robust**

- ▶ Is the model relatively immune to errors in the input data?

▶ **General**

- ▶ Does the model apply to a wide variety of situations?

▶ **Fruitful**

- ▶ Are the conclusions useful?
- ▶ Does the model inspire other good models?

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Definition: A model is **accurate** if the answers it gives are correct.

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Example. Determining projected student populations.

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This year, there are 10 million people between 18–22 years old. (P)

This year, there are 5 million students. (S)

We might conjecture that in general, $S = 0.5P$.

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Model Assumption 1:

Model Assumption 2:

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Model Assumption 1: Each college student is in 18–22 year old range.

Model Assumption 2: One of every two is enrolled in college.

If next year there are projected to be 11,000,000 18–22 year olds, we would estimate the college population to be of size $E =$ _____.

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If next year there are projected to be 11,000,000 18–22 year olds, we would estimate the college population to be of size $E = \underline{\hspace{2cm}}$.

If this value is close to correct, we say our model is accurate.

Otherwise, the model is **inaccurate**.

Problem:

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Question: Is this model descriptively realistic?

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Example. A more descriptively realistic model would incorporate other age groups. Replace Assumptions 1 and 2 by:

Model Assumption 3: College students are either:

- ▶ 18–22 (P_a of these)
- ▶ 23 or older (P_b of these)
- ▶ 17 or younger (P_c of these)

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Model Assumption 4: The enrolled percentages for each age range is:

- ▶ 30% for people aged 18–22
- ▶ 3% for people aged 23 or older
- ▶ 1% for people aged 17 or younger

We would estimate the college population to be of size

$$E = 0.3P_a + 0.03P_b + 0.01P_b.$$

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Circle one: The enrollment models are precise imprecise. Why?

Keep **Assumption 1**: Each college student is in 18–22 year old range.

Revise **Assumption 2***: The percentage of 18–22 year olds in college is between 46% and 50%. (Historically)

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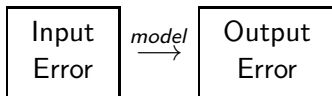
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This model is imprecise, but perhaps more helpful than the precise answer from before.

Robustness and Percentage Error

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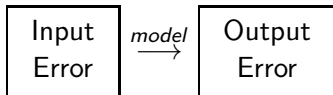
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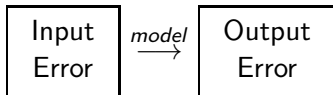


Example. If our population estimate (input) has an error of 10%, how much does our college enrollment estimate (output) change?

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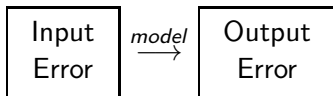
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Ask: Is the output error less than 10% or more than 10%?

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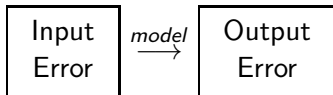
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- ▶ Some models **magnify** the errors that exist in the input data; we say these models are **sensitive to error** or **not robust**.

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Make sure we understand: What does 10% error mean?

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Recall: Population Estimate $P' = 11,000,000$.

Calculating the true population P based on a +5% error in P' :

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$$\begin{aligned}\frac{11,000,000 - P}{P} = 0.05 &\implies 11,000,000 - P = 0.05P \implies \\ 11,000,000 = 1.05P &\implies P = 10,475,190\end{aligned}$$

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Note: The true population P is **less** than the estimate P' because our estimate was 5% **too high**.

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How does this impact the true student enrollment E ?

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This highlights the principle of “Error In equals Error Out”

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Suppose that we prepare for a $\pm 10\%$ error in each population P_i , where the true values are: $P_a = 10$ mil., $P_b = 90$ mil., $P_c = 50$ mil.

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If each pop. est. P_i is a 10% **overestimate** of the true value P'_i , $P'_a = 11$, $P'_b = 99$, and $P'_c = 55$.

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Then comparing the true enrollment to the estimated enrollment E' :

$$E = 0.3(10) + 0.03(90) + 0.01(50) = 6.2$$

$$E' = 0.3(11) + 0.03(99) + 0.01(55) = 6.82$$

Percentage error: $\frac{6.82-6.2}{6.2} = \frac{.62}{6.2} = 10\%$;

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Alternatively, P_a' 10% **underestimate**, and P_b' , P_c' 10% **overestimate**:
 $P_a' = 9$, $P_b' = 99$, and $P_c' = 55$.

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Percentage error: $\frac{6.22-6.2}{6.2} = \frac{.02}{6.2} = 0.3\%$.

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Suppose that Queens College has 20,000 students and suppose that Private UNnamed Kansas College has 2,000 students this year.

If the year-to-year change in 18–22 year old population is 10%, then QC would gain 2,000 students while PUNK College would gain 200.

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The projected enrollment in all colleges would be:

$$\begin{aligned} E &= (1.1)S_1 + (1.1)S_2 + \cdots + (1.1)S_n \\ &= (1.1)(S_1 + S_2 + \cdots + S_n) \\ &= (1.1)S \end{aligned}$$

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This model is more general because it applies to individual colleges.

Fruitfulness

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- ▶ Its conclusions are useful.
- ▶ It inspires other good models.

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- ▶ Its conclusions are useful.
- ▶ It inspires other good models.

Our college enrollment model is fruitful in multiple ways:

- ▶ Planning for demand for educational grants, dormitory space, teacher hiring, etc.
- ▶ The ideas we implemented are transferrable to other situations.

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Example. How many automobiles would be junked in a given year?

- ▶ Cars play the role of people.
- ▶ Partitioning by age of cars gives better results

The Advantage of Inaccuracy

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Often accuracy is very expensive (either computationally or financially).

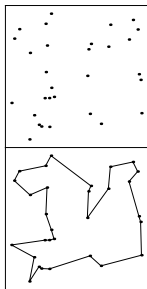
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Example. The Traveling Salesman Problem

TSP: Given a home location and a set of places to visit, find the shortest path that starts and ends at home and visits each of the places along the way.



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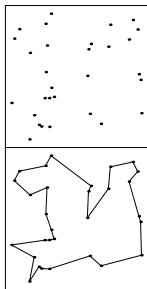
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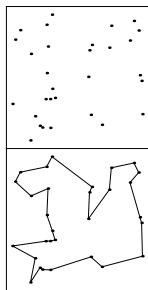
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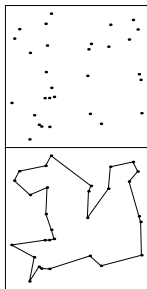
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- ▶ If you visit the same places every day, run the expensive model **once initially** in order to save money in the long run.
- ▶ If you visit different places every day, run the inexpensive algorithm daily. (Unless you're UPS or FedEx.)

