

Name: _____

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Mutliple Choice

1. Which of the following is *not* a field?

- (a) The numbers $\{0, 1\}$ with $+$ and \times defined modulo 2
- (b) The natural numbers \mathbb{N}
- (c) The real numbers \mathbb{R}
- (d) The complex numbers \mathbb{C}

2. The multiplicative inverse of $1 + i$ is

- (a) $\frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}}i$
- (b) $1 - i$
- (c) $\frac{i}{2}$
- (d) $\sqrt{2} - \sqrt{2}i$
- (e) $\frac{1}{2} - \frac{1}{2}i$

3. Which number satisfies $z^8 = 1$?

- (a) $z = \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}}i$
- (b) $z = 1 - i$
- (c) $z = \frac{i}{2}$
- (d) $z = \sqrt{2} - \sqrt{2}i$
- (e) $z = \frac{1}{2} - \frac{1}{2}i$

4. Consider the vector space \mathbb{R}^4 . Which one of the following subsets is a subspace?

- (a) $\{(a, b, c, d) \in \mathbb{R}^4 : a = 1\}$
- (b) $\{(a, b, c, d) \in \mathbb{R}^4 : a + b + c + d = 1\}$
- (c) $\{(a, b, c, d) \in \mathbb{R}^4 : a + 2b = 3c + 4d\}$
- (d) $\{(a, b, c, d) \in \mathbb{R}^4 : a + b + c \geq d\}$
- (e) $\{(a, b, c, d) \in \mathbb{R}^4 : ab = cd\}$
- (f) $\{(a, b, c, d) \in \mathbb{R}^4 : a^2 + b^2 + c^2 + d^2 = 1\}$

True or False

5. The set $\left\{ f : [0, 1] \rightarrow \mathbb{R} : f \text{ is integrable and } \int_0^1 f = 0 \right\}$ is a subspace of $\mathbb{R}^{[0,1]}$.
6. The set $\{f : (-1, 1) \rightarrow \mathbb{R} : f \text{ is twice differentiable and } f''(0) = 2\}$ is a subspace of $\mathbb{R}^{(-1,1)}$.
7. The set $\{f : \mathbb{R} \rightarrow \mathbb{R} : f'(-1) = f(1)\}$ is a subspace of $\mathbb{R}^{\mathbb{R}}$.
8. The set of all sequences of real numbers with limit 0 is a subspace of \mathbb{R}^{∞} .
9. If $X = \{(a, 2a, 3a) \in \mathbb{R}^3 : a \in \mathbb{R}\}$ and $Y = \{(a, a, a) \in \mathbb{R}^3 : a \in \mathbb{R}\}$ then $(1, 3, 5) \in X + Y$.
10. If $X = \{(0, 0, a) \in \mathbb{R}^3 : a \in \mathbb{R}\}$, $Y = \{(a, a, a) \in \mathbb{R}^3 : a \in \mathbb{R}\}$ and $Z = \{(a, a, b) \in \mathbb{R}^3 : a, b \in \mathbb{R}\}$, then $X \oplus Y = Z$.